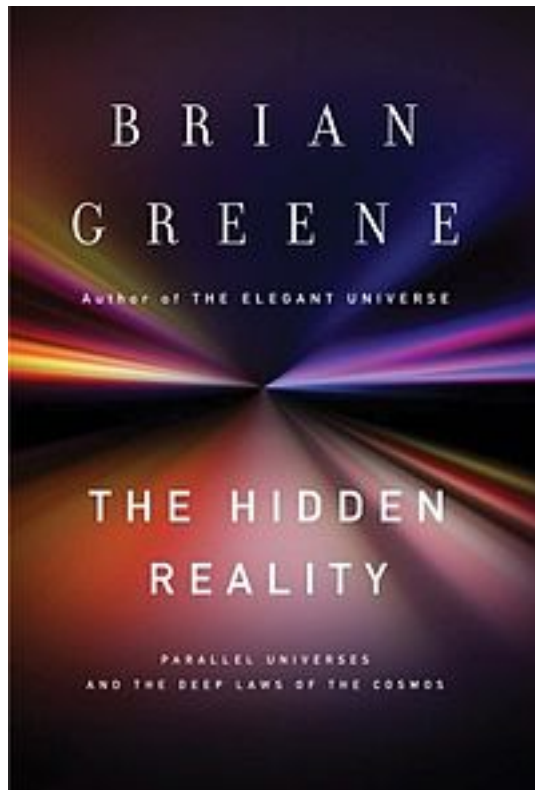


Brian Greene, Nov 6 @ 7pm

Elliott Hall of Music



Free seating pass required for entry

<http://www.convocations.org/portfolio/brian-greene-11-6-14/#sthash.KqvAENA9.dpuf>

Last Time

- Ohm's Law
- Series and Parallel Resistors
- Series and Parallel Capacitors

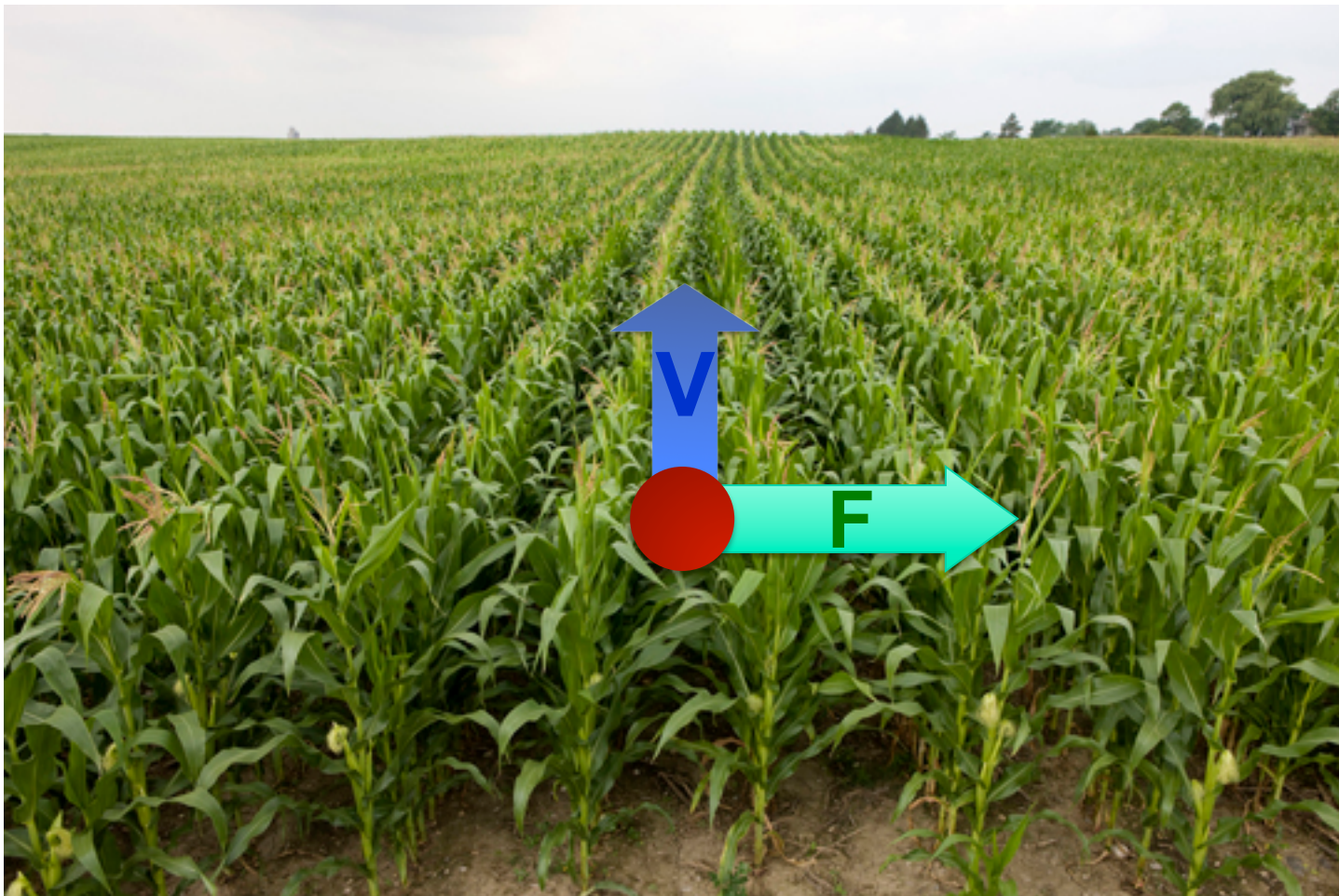
Today

- Ohm's Law
- Series and Parallel Resistors
- Series and Parallel Capacitors

Magnetic Force on a Charge

$$\vec{F}_{\text{magnetic}} = q\vec{v} \times \vec{B}$$

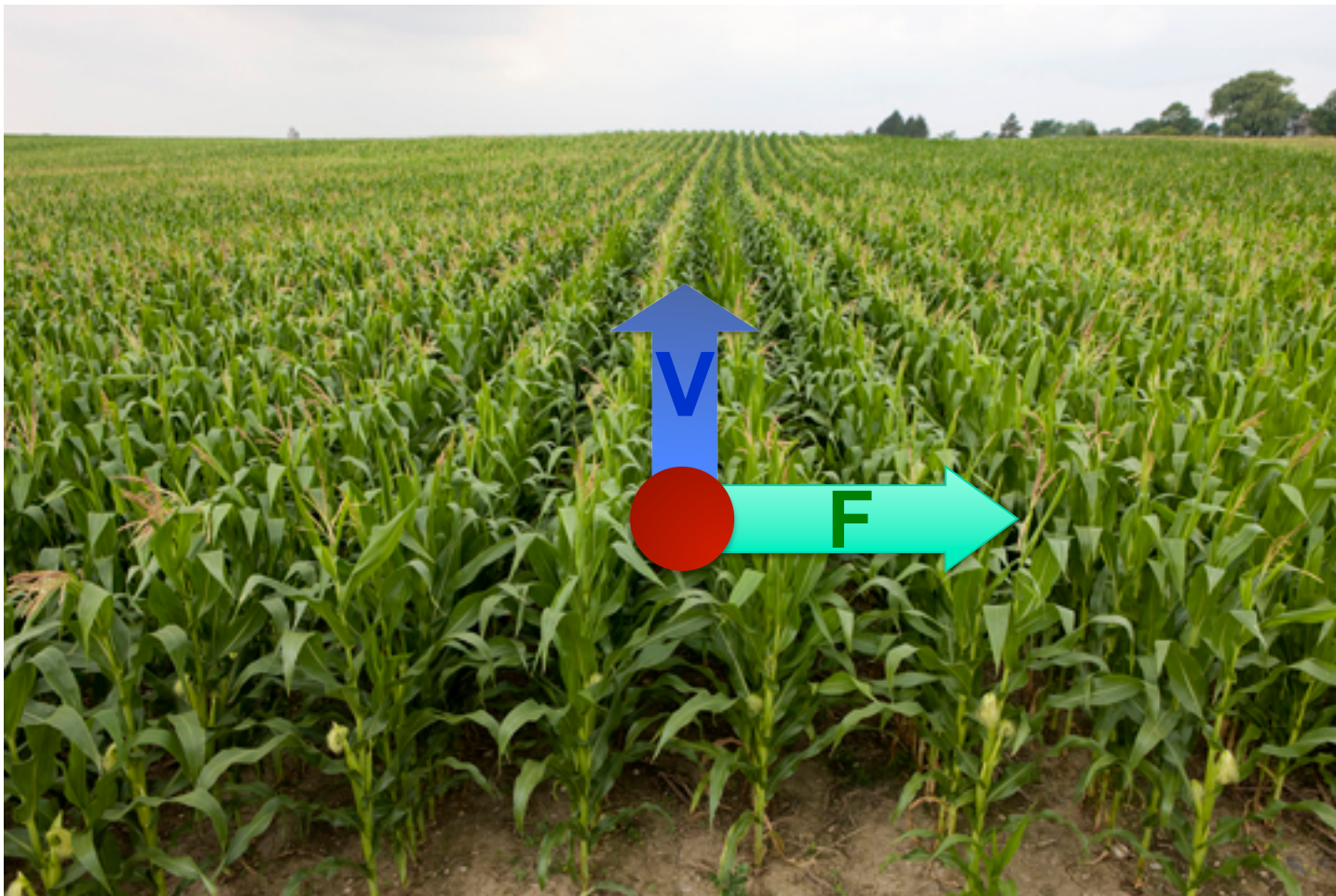
A proton walks into a Corn Field/Magnetic Field.
Which way the force point?



Magnetic Force on a Charge

$$\vec{F}_{\text{magnetic}} = q\vec{v} \times \vec{B}$$

Force ALWAYS perpendicular to velocity.
Where else have you seen this?



Magnetic Force on a Charge

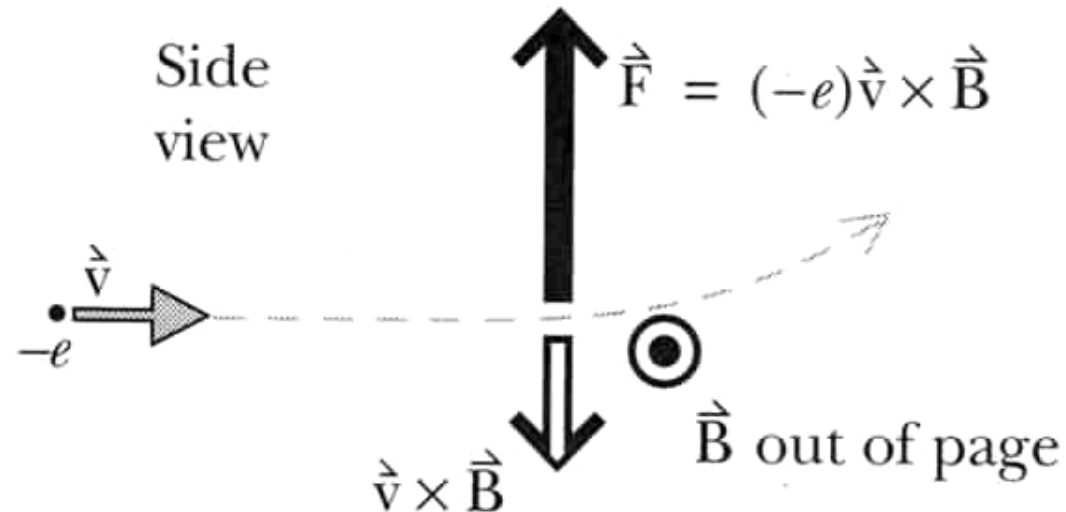
$$\vec{F}_{\text{magnetic}} = q\vec{v} \times \vec{B}$$

An electron walks into a Corn Field/Magnetic Field.
Which way the force point?



Magnetic Force on a Charge

$$\vec{F}_{\text{magnetic}} = q\vec{v} \times \vec{B}$$



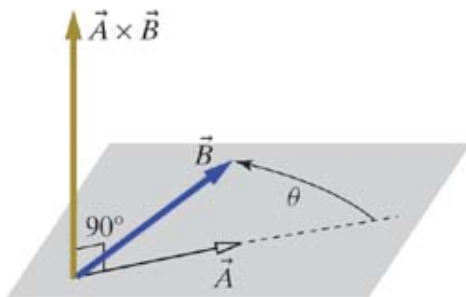
Electron charge = $-e$:

The magnetic force on a moving electron is in opposite direction to the direction of the cross product $\vec{v} \times \vec{B}$

Right-Hand Rule

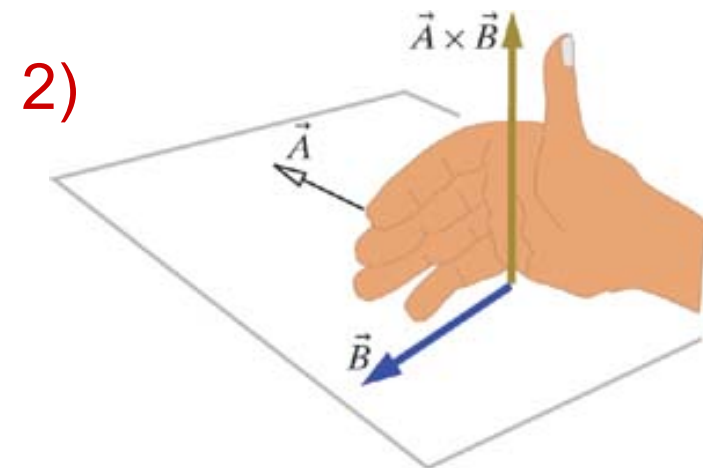
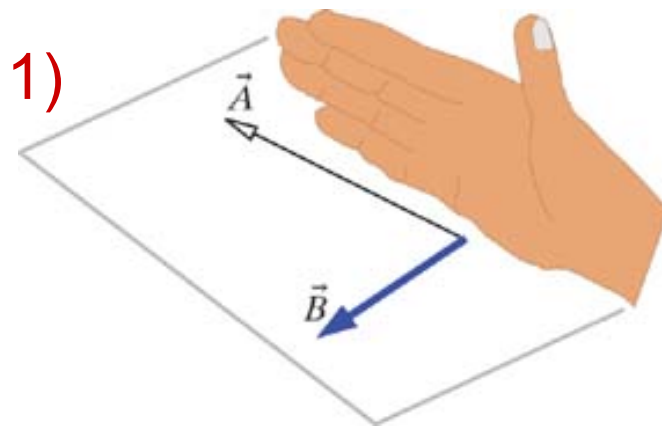
$$\vec{F}_{\text{mag}} = q\vec{v} \times \vec{B}$$

MAGNETIC FORCE
point charge

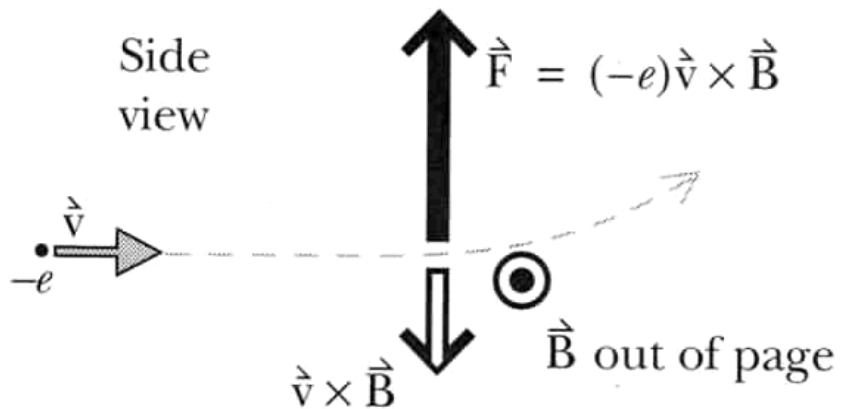


Result of Cross Product $\vec{v} \times \vec{B}$
is Perpendicular to both \vec{v} and \vec{B}

Right-Hand Rule:



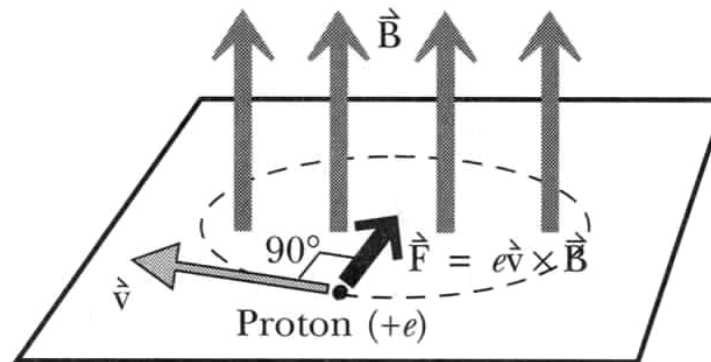
Motion in a Magnetic Field



$$\vec{F}_{\text{magnetic}} = q\vec{v} \times \vec{B}$$

What if we have large (infinite) area with constant $\vec{B} \perp \vec{v}$

$$\left| \frac{d\vec{p}}{dt} \right| = qvB$$



Determining the Momentum of a Particle

Position vector r : $\left| \frac{d\vec{r}}{dt} \right| = v = \omega r \rightarrow \omega = \frac{v}{r}$ Circular motion

$$\left| \frac{d\vec{p}}{dt} \right| = \omega p = \left(\frac{v}{r} \right) p \qquad \left| \frac{d\vec{p}}{dt} \right| = |q|vB$$

$$\left(\frac{v}{r} \right) p = |q|vB$$

$$p = |q|Br \quad \leftarrow \text{valid even for relativistic speeds}$$

Used to measure momentum in high-energy particle experiments

Circular Motion at any Speed

$$\vec{F}_{\text{magnetic}} = q\vec{v} \times \vec{B}$$

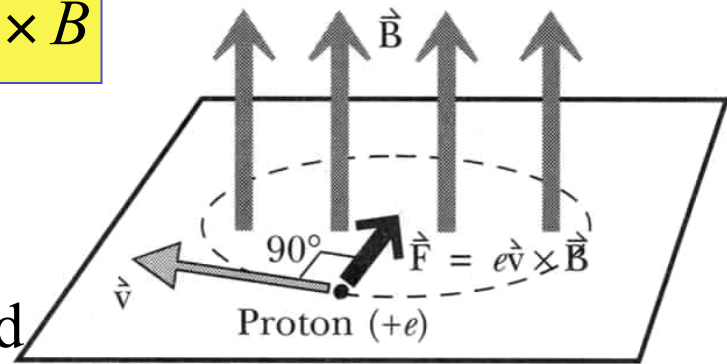
Any rotating vector:

$$\left| \frac{d\vec{X}}{dt} \right| = \omega |\vec{X}| \quad \omega \dots \text{angular speed}$$

$$\left| \frac{d\vec{p}}{dt} \right| = \omega |p|$$

$$\omega \frac{mv}{\sqrt{1 - v^2 / c^2}} = |q|vB$$

$$\left| \frac{d\vec{p}}{dt} \right| = |q\vec{v} \times \vec{B}| = |q|vB \sin 90^\circ$$



$$\omega = \frac{|q|B}{m} \sqrt{1 - v^2 / c^2}$$

Cyclotron Frequency

Circular Motion at Low Speed

$$\omega = \frac{|q|B}{m} \sqrt{1 - v^2 / c^2}$$

if $v \ll c$: $\omega = \frac{|q|B}{m}$

independent of v !

Alternative derivation:

$$F = ma$$

$$|q|vB \sin 90^\circ = m \frac{v^2}{R}$$

$$|q|B = m\omega \longrightarrow$$

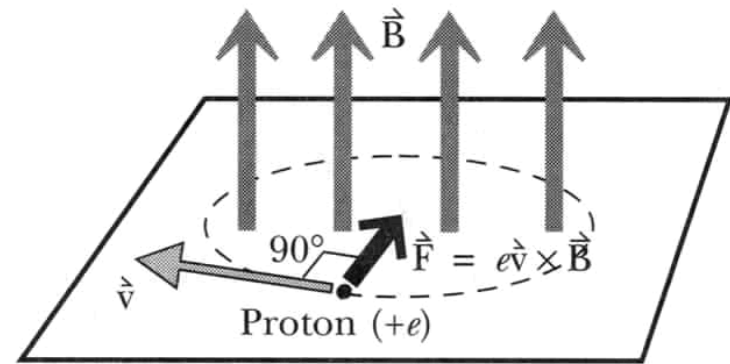
$$\omega = \frac{|q|B}{m}$$

Period T :

$$\omega = \frac{2\pi}{T} \longrightarrow$$

$$T = 2\pi \frac{m}{|q|B}$$

Non-Relativistic



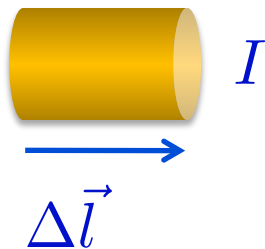
Biot-Savart Law



$$\vec{B} = \left(\frac{\mu_o}{4\pi} \right) \frac{q\vec{v} \times \hat{r}}{|\vec{r}|^2}$$

BIOT-SAVART LAW
point charge

We need to understand
how these are related



$$\vec{B} = \left(\frac{\mu_o}{4\pi} \right) \frac{I \Delta \vec{l} \times \hat{r}}{|\vec{r}|^2}$$

BIOT-SAVART LAW
current in a wire

$\Delta \vec{l}$ = length of this
chunk of wire

Blast from the Past:
Lecture 12

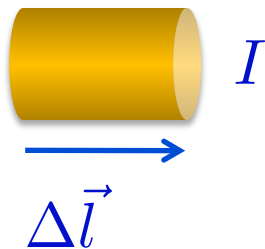
Magnetic Force on a charge or wire



$$\vec{F}_{\text{mag}} = q\vec{v} \times \vec{B}$$

**MAGNETIC FORCE
point charge**

We need to understand
how these are related



$$\Delta \vec{F}_{\text{mag}} = I \Delta \vec{l} \times \vec{B}$$

**MAGNETIC FORCE
current in a wire**

$\Delta \vec{l}$ = length of this
chunk of wire

GOAL: Show $q\vec{v} \longrightarrow I\Delta\vec{l}$

(point charge) (wire)

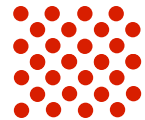
(POSITIVE)
POINT CHARGE



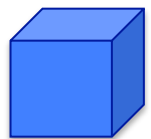
$$q\vec{v}$$

$$q\vec{v}$$

MANY POINT
CHARGES



N particles



ΔV

$$n = \left[\frac{\#}{m^3} \right] \text{ particles per volume } \Delta V$$

$$Nq\vec{v}$$



$$(n\Delta V)q\vec{v}$$

CHUNK
OF WIRE



I



$\Delta\vec{l}$ = length of this chunk of wire

Move the vector symbol

$$q\vec{v}n\Delta V = q\vec{v}nA\Delta l$$

$$= \underbrace{q|v|nA}_{\equiv I} \Delta\vec{l} \quad I\Delta\vec{l}$$

Blast from the Past:
Lecture 12

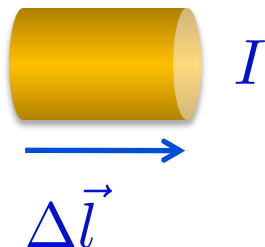
Magnetic Force on a charge or wire



$$\vec{F}_{\text{mag}} = q\vec{v} \times \vec{B}$$

MAGNETIC FORCE
point charge

We just showed how
these are related



$$\Delta \vec{F}_{\text{mag}} = I \Delta \vec{l} \times \vec{B}$$

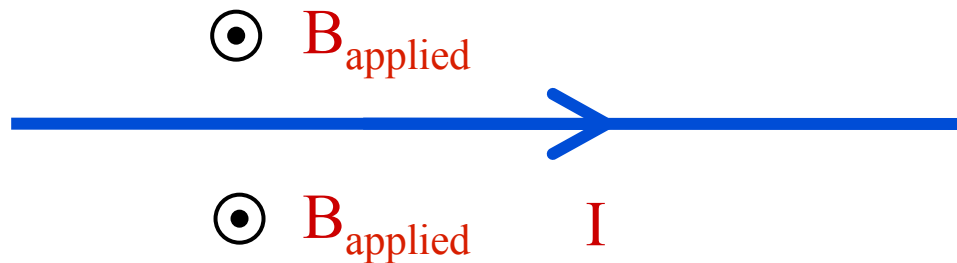
MAGNETIC FORCE
current in a wire

$\Delta \vec{l}$ = length of this
chunk of wire

Magnetic Force on a Wire

$$\Delta \vec{F}_{\text{mag}} = I \Delta \vec{l} \times \vec{B}$$

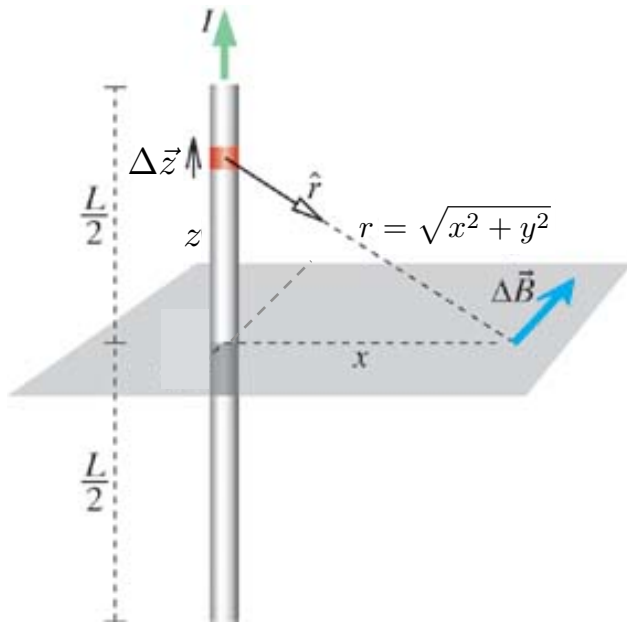
Current-carrying wire in an applied magnetic field B



Which way will the wire move?

Magnetic Field of a Straight Wire

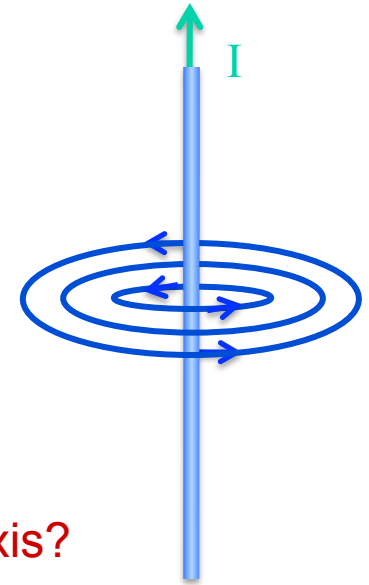
$$|B_z| = \left(\frac{\mu_o}{4\pi} \right) \frac{IL}{x \sqrt{x^2 + (L/2)^2}} \quad \text{B in the bisecting plane}$$



Which direction does B point?

→ Always along concentric circles

In cylindrical coordinates, it points in the " $\hat{\theta}$ " direction



Will the y axis look different from the x axis?

No, so we can trade $x \rightarrow r$

$$\vec{B} = \left(\frac{\mu_o}{4\pi} \right) \frac{IL}{r \sqrt{r^2 + (L/2)^2}} \hat{\theta}$$

B of a Long Straight Wire
(cylindrical coord.)

Blast from the Past:
Lecture 13

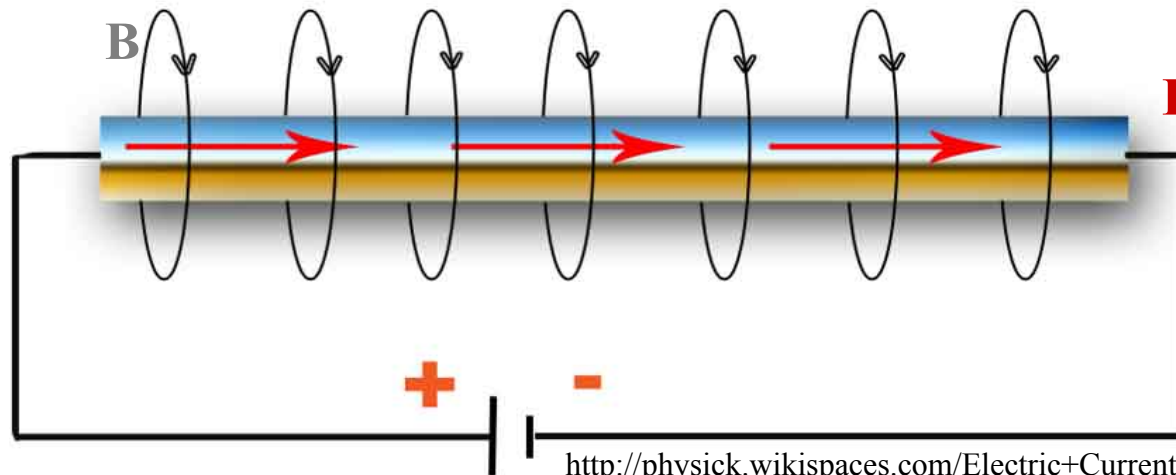
Very Close to the Wire

$$\vec{B} = \left(\frac{\mu_o}{4\pi} \right) \frac{IL}{r\sqrt{r^2 + (L/2)^2}} \hat{\theta}$$

Very close to the wire: $r \ll L$ $\sqrt{r^2 + (L/2)^2} \approx L/2$

$$\Rightarrow \vec{B} = \left(\frac{\mu_o}{4\pi} \right) \frac{IL}{r(L/2)} \hat{\theta} = \left(\frac{\mu_o}{4\pi} \right) \frac{2I}{r} \hat{\theta} = \vec{B}$$

**CLOSE TO
THE WIRE**



<http://physick.wikispaces.com/Electric+Current>

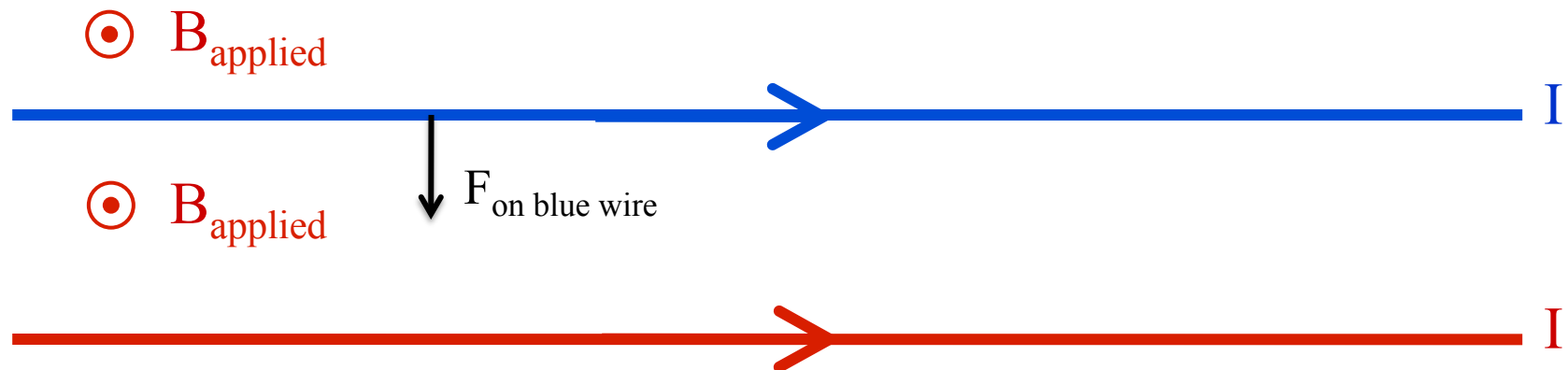
Blast from the Past:
Lecture 13

Force Between Parallel Wires

$$\Delta \vec{F}_{\text{mag}} = I \Delta \vec{l} \times \vec{B}$$

$$\vec{B} = \left(\frac{\mu_o}{4\pi} \right) \frac{2I}{x} \hat{\theta}$$

B_{applied} = Magnetic field applied by the **red** wire. **Blue** wire feels a force down.



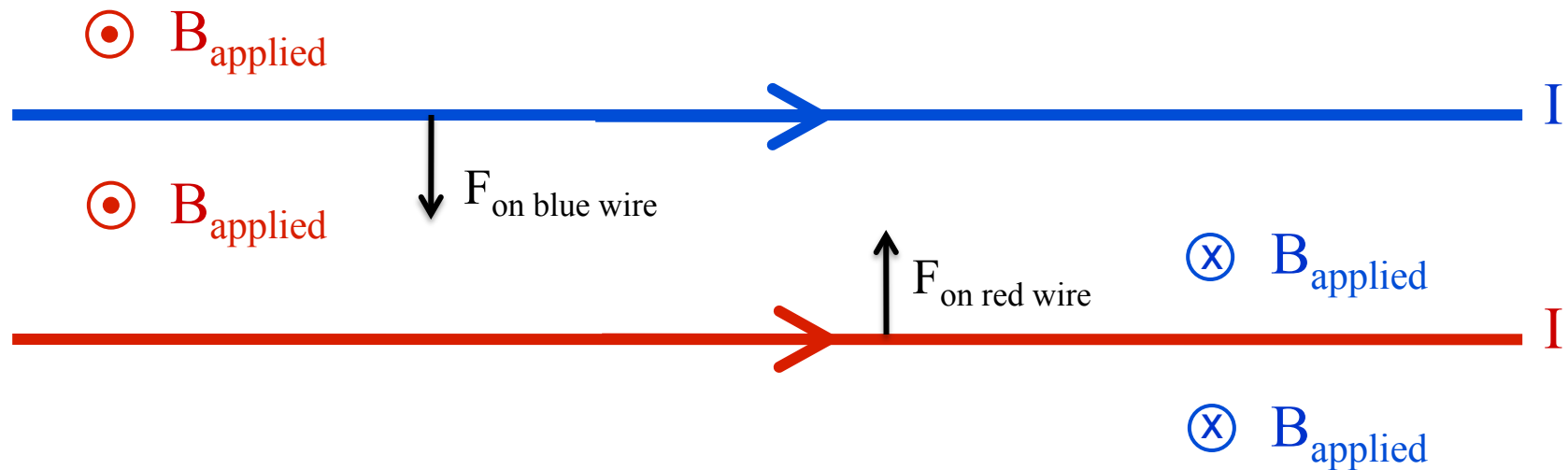
What about reciprocity? (Equal and opposite forces)

Force Between Parallel Wires

$$\Delta \vec{F}_{\text{mag}} = I \Delta \vec{l} \times \vec{B}$$

$$\vec{B} = \left(\frac{\mu_o}{4\pi} \right) \frac{2I}{x} \hat{\theta}$$

B_{applied} = Magnetic field applied by the **red** wire. **Blue** wire feels a force down.



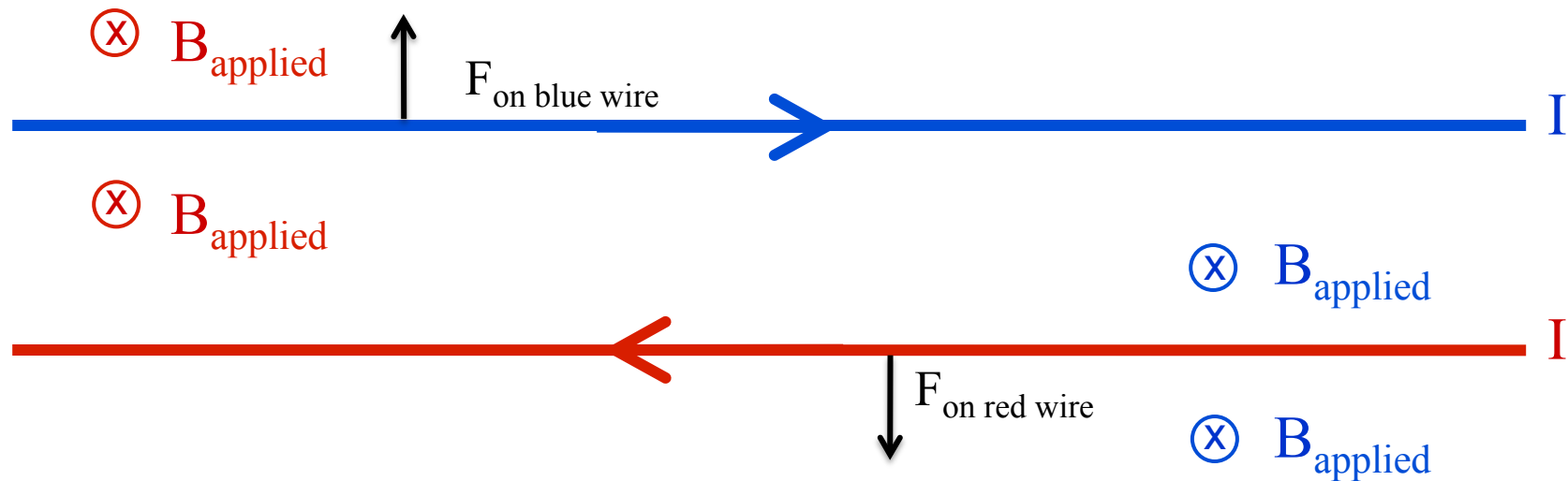
B_{applied} = Magnetic field applied by the **blue** wire. **Red** wire feels a force up.

Force Between (Anti) Parallel Wires

$$\Delta \vec{F}_{\text{mag}} = I \Delta \vec{l} \times \vec{B}$$

$$\vec{B} = \left(\frac{\mu_o}{4\pi} \right) \frac{2I}{x} \hat{\theta}$$

B_{applied} = Magnetic field applied by the **red** wire. **Blue** wire feels a force up.



B_{applied} = Magnetic field applied by the **blue** wire. **Red** wire feels a force down.

Hall Effect

By measuring the Hall effect for a particular material,
we can determine the sign of the moving particles
that make up the current

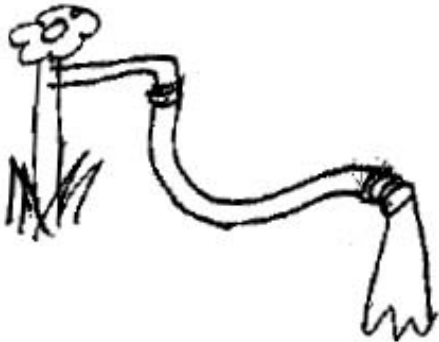
Why would it be anything other than electrons? (Negative charges)

Semiconductors: sometimes current is carried by electrons,
but sometimes it is carried by the "holes".

In **semiconductors**, "holes" (missing electrons)
in the electron sea behave like positive charges.

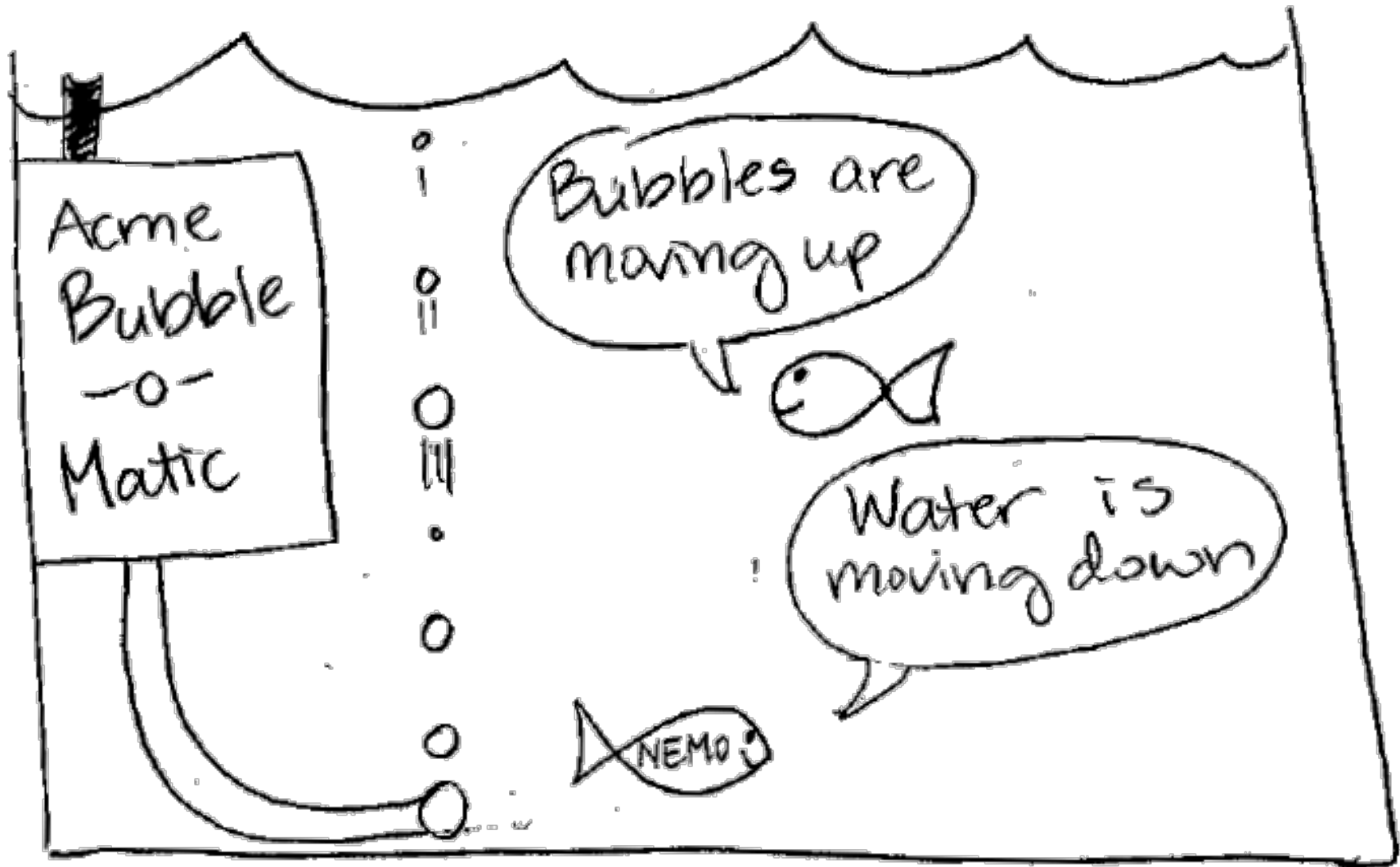
ZEN KOAN

Water from a hose



Zen riddle: Is water coming out of the hose, or is the absence of water moving into the hose?

“Holes” not useful here

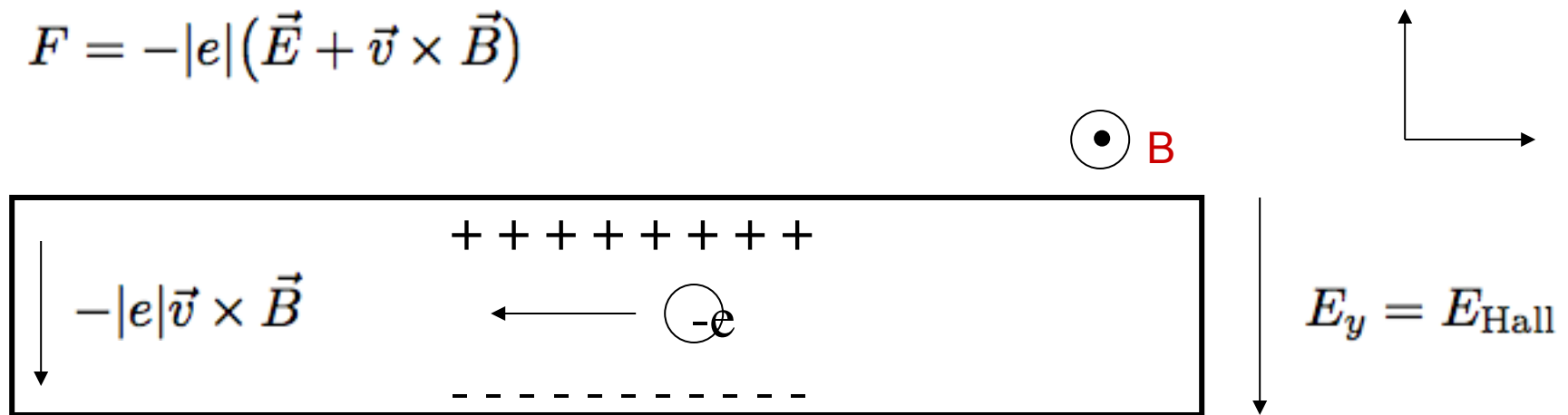


“Holes” useful here

In a semiconductor, "Holes" in the electron sea act like positive charges.

Hall Effect and Electrons

$$\vec{F} = -|e|\hbar{(\vec{E} + \vec{v} \times \vec{B})}$$



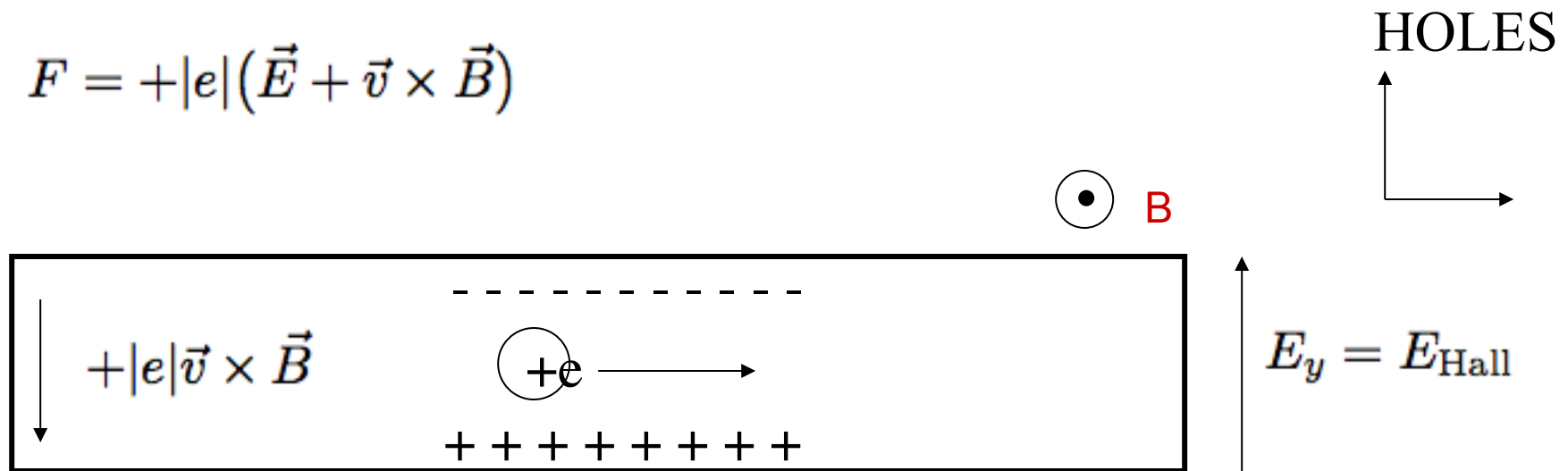
\Rightarrow

$$E_y = E_{\text{Hall}}$$

E_{Hall} points down
due to buildup of charge.

Hall Effect and Holes

$$F = +|e|(\vec{E} + \vec{v} \times \vec{B})$$



$$E_y = E_{\text{Hall}}$$

E_{Hall} points up due to
buildup of charge.

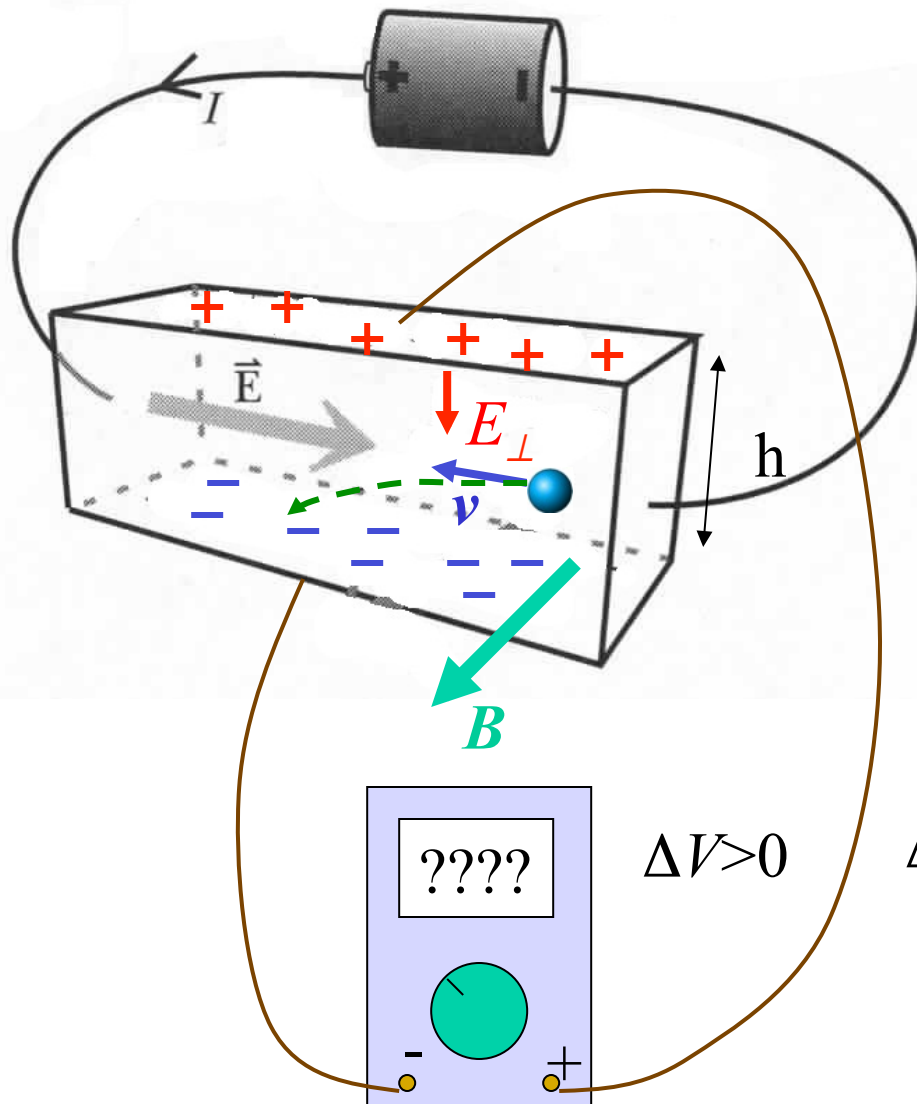
Hall Effect

$$\vec{F} = q\vec{E} + q\vec{v} \times \vec{B}$$

$$\vec{F}_{e\perp} + \vec{F}_B = 0$$

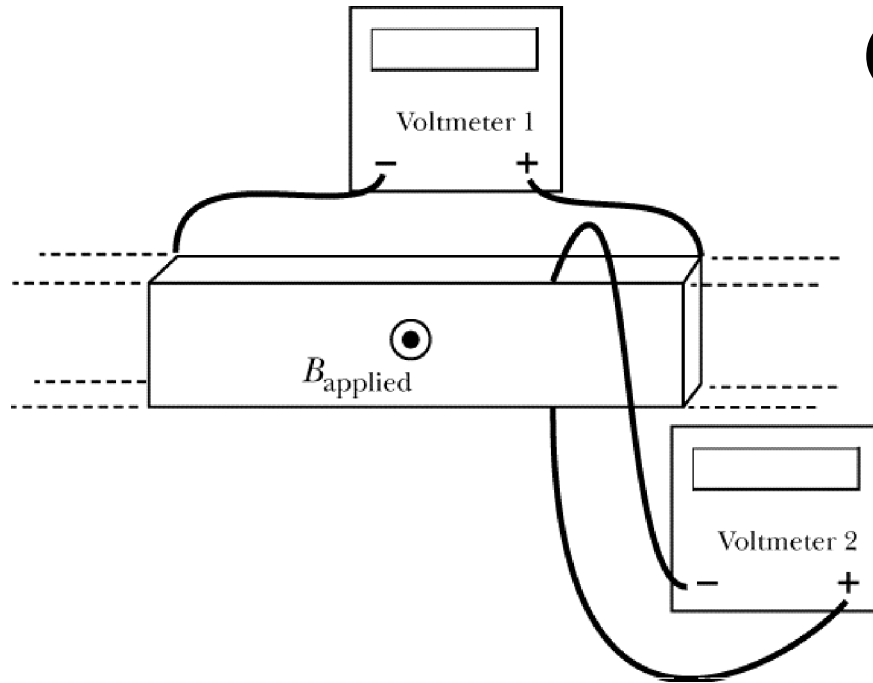
$$e\vec{E}_{e\perp} = -e\vec{v} \times \vec{B}$$

$$E_{e\perp} = \bar{v}B$$



$$\Delta V = E_{e\perp}h = \bar{v}Bh$$

Clicker Question



Voltmeter 1 reading is POSITIVE
Voltmeter 2 reading is POSITIVE

Mobile charges are:

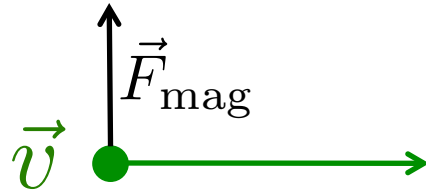
- A) Positive (holes)
- B) Negative (electrons)
- C) Not enough information

iClicker

$$\vec{F}_{\text{mag}} = q\vec{v} \times \vec{B}$$

MAGNETIC FORCE
point charge

Proton



\otimes B_{applied}

In which direction does \vec{F}_{mag} point for the **proton**?

- A) Up
- B) Down
- C) Into the Board
- D) Out of the Board

iClicker

$$\vec{F}_{\text{mag}} = q\vec{v} \times \vec{B}$$

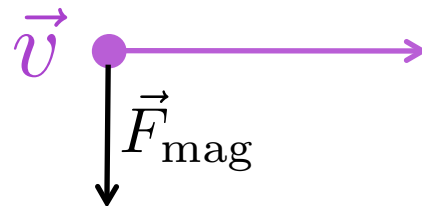
MAGNETIC FORCE
point charge

Proton



\otimes B_{applied}

Electron



- A) Up
- B) Down
- C) Into the Board
- D) Out of the Board

In which direction does \vec{F}_{mag} point for the **electron**?

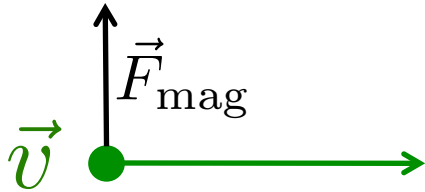
Hall Effect

$$\vec{F}_{\text{mag}} = q\vec{v} \times \vec{B}$$

MAGNETIC FORCE
point charge

A **hole** in the electron sea
behaves like a **proton**.

Proton
or "Hole"



⊗ B_{applied}

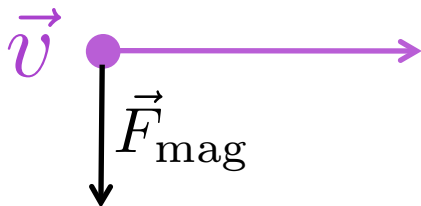
Inside a Material:



Moving **holes**
get pushed
to the top

⊗ B_{applied}

Electron



Moving **electrons**
get pushed
to the bottom

Hall Effect

$$\vec{F}_{\text{mag}} = q\vec{v} \times \vec{B}$$

MAGNETIC FORCE
point charge

A **hole** in the electron sea
behaves like a **proton**.

Inside a Material:

Moving **holes**
get pushed
to the top



$\Delta V = \text{Hall Voltage}$

\otimes B_{applied}

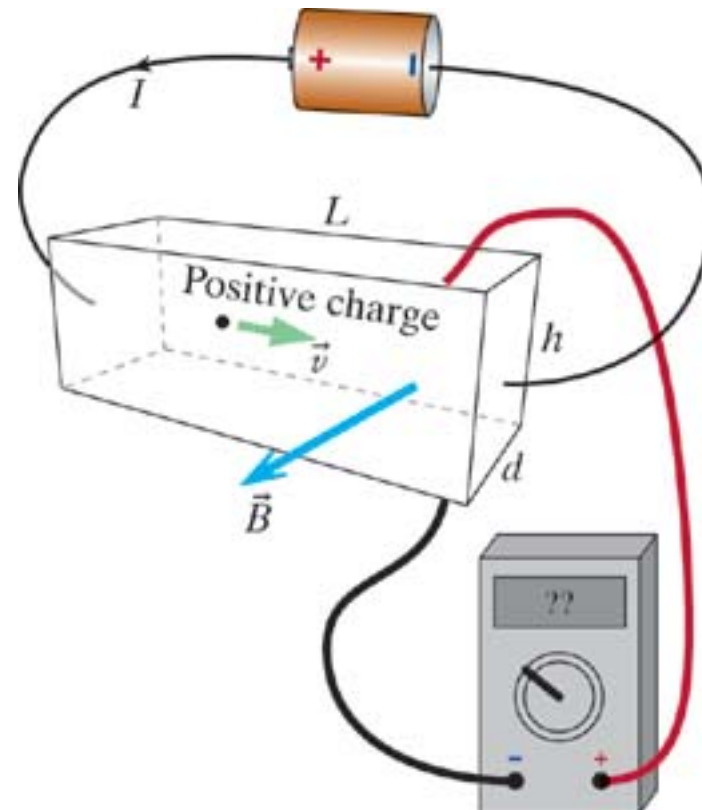
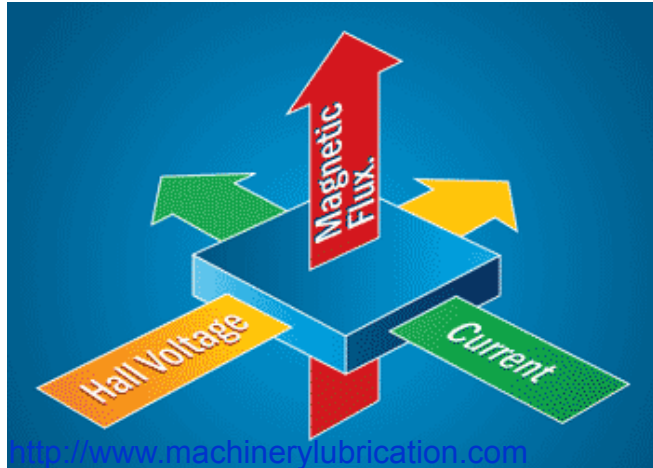
How long does this go on?
→ Until the Hall Voltage
is strong enough to balance
the magnetic force \vec{F}_{mag}

Moving **electrons**
get pushed
to the bottom



$\Delta V = \text{Hall Voltage}$

Measuring the Hall Effect



1. Apply B-Field
2. Apply Current I
3. Measure "Hall Voltage"